

SPATIAL VARIABILITY OF SNOW ACCUMULATION ON VERNAGTFERNER,
AUSTRIAN ALPS, IN WINTER 2003/2004

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ABSTRACT

In this paper the snow accumulation pattern on Vernagtferner is analyzed. The measurements of snow depth and snow density were carried out at the end of the glaciological winter period 2003/2004. The values of snow depth are particularly reliable because the summer 2003 with its high ablation rates left a dense surface layer that was easy to detect with snow poles even in the upper firn area. The snow accumulation pattern is statistically analyzed regarding its relationship with topography and wind regime. A generalized-least-squares regression is applied using geomorphometric attributes representing measures of local wind sheltering. The main wind direction for winter 2003/2004 is derived from data of two meteorological stations in the catchment and used for directional parameters. It could be shown that in the lower areas between 2750 and 3050 m a.s.l. elevation is the predominant factor influencing the amount of snow accumulation. Above 3050 m a.s.l., redistribution by wind is the decisive factor both regarding snow

erosion and accumulation. The results are applied in a regionalization procedure with universal kriging.

ZUSAMMENFASSUNG

In dieser Arbeit soll eine Auswertung der räumlichen Schneeakkumulation am Vernagtferner vorgestellt werden. Die Messungen von Schneetiefe und Schneedichte erfolgten zum Ende des glaziologischen Winterhalbjahres 2003/2004. Die besonders günstigen Bedingungen für getreue Messwerte der Schneetiefe entstanden aufgrund der hohen Schmelzraten im vorangegangenen Sommer 2003. In Folge dessen war der Vorjahreshorizont, durch seine hohe Dichte, bei der Messung mit Schneetiefensonden auch in den höheren Firnlagen gut zu erkennen.

Das Schneeakkumulationsmuster wird statistisch ausgewertet und in Beziehung zu verschiedenen Einflussfaktoren, wie Topographie und Wind gesetzt. Dabei wird eine generalized-least-squares Regression angewandt, welche geomorphometrische Eigenschaften verwendet, die ein Maß für das lokale wind sheltering darstellen. Die vorherrschende Windrichtung für das Winterhalbjahr 2003/2004 wird anhand von Daten zweier meteorologischer Stationen im Einzugsgebiet bestimmt und als gerichtetes Parameter angewendet. Es konnte gezeigt werden dass in den unteren Höhenlagen zwischen 2750 und 3050 m über NN ist die Höhenlage selbst der wesentliche Einflussfaktor für die Schneeakkumulation. Oberhalb von 3050 m über NN dominiert der Einfluss aus Windverdriftungen, mit Schneerosion und Schneeablagerung. Die Ergebnisse der Analyse finden in einer Regionalisierung mittels universellem Kriging Anwendung.

Keywords: Glacier mass balance, snow redistribution, geomorphometry, geostatistical modelling

1. INTRODUCTION

Since 1964/65 the Commission for Glaciology at the Bavarian Academy of Sciences has been determining the distributed glacier mass balance of Vernagtferner, resulting in measurements of winter and summer mass balance (Escher-Vetter et al., 2004). The photogrammetric and hydrological method are used complementarily for this purpose (Moser, 1986). The combination of these methods allows cross-checking the results, which is especially important as the measurement of winter precipitation and its interpolation is still problematic in the high alpine region. Therefore knowledge of the winter snow accumulation, determined from the winter mass balance, is an important value for the glacier mass gain. But the snow accumulation and its specific distribution pattern also affect the ablation, and therefore the total mass balance pattern, as snow melts more slowly than ice due to differences in albedo and thermal conductivity.

For the determination of snow accumulation in the field, measurements of snow density and snow depth are taken. The assessment of winter snow accumulation on a glacier by snow depth measurements using poles often implies inaccuracies resulting from the vague identification of the previous summer horizon. This occurs especially in the upper firn area where snow remains over the summer, so that the increase in snow density is not as obvious as it is over ice, which represents the summer horizon in the ablation area. Gravimetric measurements of snow density in a snow pit are advantageous to detect the previous year's summer horizon, but require much more effort. Thus at the end of the accumulation period snow density is usually measured at few sites, whereas snow depth can be measured at many sites. From the mean snow density the snow water equivalent (SWE) can be calculated for all snow depth sample sites.

The summer 2003 with its extremely high ablation rates left a dense surface even in the upper firn basins of Vernagtferner. Thus at the end of the accumulation period in winter 2003/04, snow depth measurements profited from a well-defined base layer. Detailed measurements were taken during a field survey at the end of April 2004 in order to obtain a data base of snow accumulation at Vernagtferner.

In the past 40 years, SWE measurements used to be regionalized over the entire glacier as a polynomial function of elevation (Moser et al., 1986). This method assumes a strong correlation between SWE and elevation but in fact correlation is low in most cases. In the present work, the spatial distribution of detailed SWE measurements and process-related terrain parameters computed from a digital elevation model are used to present an improved regionalization method. The analyses are intended to obtain insight into snow redistribution patterns on Vernagtferner, and to optimize sampling and estimation procedures for future work.

2. STUDY AREA

Vernagtferner is located in the Ötztal Alps in Austria at $46^{\circ}52'N$ and $10^{\circ}49'E$. The glacier currently covers 8.36 km^2 , extending from 2780 to 3628 m a.s.l. The main aspect of the slopes is to the south, but the glacier can be divided into three parts facing different directions (figure 1): Schwarzwand area facing northeast to southeast, the Taschach area exposed to southeast to southwest and the Brochkogel area with an aspect ranging from south to west (Reinwarth and Escher-Vetter, 1999). These areas have different altitudinal extent and size. Schwarzwand area and Brochkogel area both comprise about 2 km^2 , whereas Taschach area extends over about 4.5 km^2 and has two accumulation areas that merge into one glacier tongue.

The Vernagt basin extends over an area of 11.4 km² down to the gauging station at 2635 m a.s.l. Based on the calculation of water balance components of the Vernagt basin, the mean precipitation of 1974–2002/03 was determined to be 1381 mm, with a winter precipitation of 892 mm (Escher-Vetter et al., 2004). All winter precipitation in the catchment is in the form of snow. In terms of mass balance, winter precipitation varies very little between the years compared to summer ablation (Escher-Vetter et al., 2004).

3. METHODOLOGY

3.1 Field measurements

The direct glaciological method is conducted using a fixed date system. Therefore measurement of winter balance is carried out at the end of the glaciological winter mid-year. During the field work from 29 April to 2 May 2004, 480 measurements of snow depth serving 165 sample sites were taken at Vernagtferner, covering most of the glacier's slopes (figure 1, table 1). At each site, three snow depth measurements were taken randomly within 10 m of horizontal distance; these triple measurements were averaged. The sample sites are located along nine vertical profiles. The distance between the sample sites varied usually from 50 to 300 m within the same profile. Snow density was measured gravimetrically at five snow pits located between 2940 and 3260 m a.s.l. (figure 1). The coordinates of all sample sites were recorded by GPS.

Field experience of past years shows that the spatial variability of snow depths is greater than that of snow density which corresponds to findings elsewhere (Elder et al., 1989). A comparison of densities measured at five GPS-referenced sites between 2001 and 2004 shows that there is no clear altitudinal trend, while inter-annual variation of average snow

densities amounts to 5-10% of the values (figure 2). Due to the lack of a distinctive altitudinal pattern, the mean snow density of 2004 (0.38 g/cm^3) was uniformly used to derive values of SWE for the 165 sample sites. Thus snow depth and SWE are taken to be directly proportional.

Since snow redistribution by wind plays a major role for the spatial pattern of SWE, wind direction and speed were analyzed from data of two stations in the glacier's catchment, starting 1 October 2003 to 30 April 2004, on an hourly basis, using Thies anemometers. One of these stations is located at a gauging station below the glacier at 2635 m a.s.l., the other one at 3075 m a.s.l. at Schwarzkögele, a peak on the eastern side of Vernagtferner (figure 1). Average and maximum wind speeds were calculated for 12 classes of wind direction, and directional wind frequencies were summarized for these classes at both stations.

3.2 Terrain parameters

For the analysis of the statistical relation between snow distribution, topography and main wind direction, morphometric terrain parameters were derived from a digital elevation model (DEM) using the software ArcView 3.2, its extension DEMAT, the terrain analysis software SAGA (Version 1.1, O. Conrad, Göttingen, 2004), and own code for computing wind sheltering indices written in the data analysis environment R (R Development Core Team, 2004). The DEM with a resolution of 10 m was obtained from stereoscopic analysis of aerial photographs taken in summer 2003 within the OMEGA project (Development of Operational Monitoring System for European Glacial Areas).

In addition to the locally defined terrain parameters elevation, aspect, slope and curvature, process-related morphometric site characteristics were used. These include the horizontal distance from the ridge in windward direction (northwest), a measure of topographic wind sheltering as defined below, and potential incoming solar radiation for the months of June and December. In the case of the aspect variable, cosine transforms $\cos(\text{aspect} - \text{offset})$ were used in order to obtain an interval-scaled variable from a spherical one. Furthermore, non-linear transformation of the available variables were derived during exploratory data analysis.

Similar to a definition by Winstral et al. (2002), we use the maximum gradient within a given radius in upwind direction as a measure of topographic wind sheltering:

$$\text{Shelter index}(S) = \arctan(\max\{ (z(\mathbf{x}_0) - z(\mathbf{x})) / |\mathbf{x}_0 - \mathbf{x}| : \mathbf{x} \in S \})$$

where $S = S(\mathbf{x}_0, a, \Delta a, d)$ is the set of grid nodes within a distance $\leq d$ in the range of directions $a \pm \Delta a$ from \mathbf{x}_0 . In contrast to the original definition of Winstral et al. (2002), whose shelter index is an average of the present one for $\Delta a'$ near 0 and a' varying between our $a - \Delta a$ and $a + \Delta a$, the present definition does not depend on a specific choice of $\Delta a'$ in the implementation. Optimal azimuth and tolerance parameters were estimated by numerically minimizing the residual standard error in the presence of the other relevant model parameters.

3.3 Geostatistical analysis

The statistical relation between SWE and terrain parameters was analyzed using a generalized-least-squares linear regression model in conjunction with an exponential model

of spatial autocorrelation. The generalized least-squares approach was chosen since ordinary least-squares models are not able to account for the autocorrelation structure that is inherent to spatial data. Ordinary regression would therefore yield biased variance estimates and invalid p-values in the presence of autocorrelation. Model variables were selected manually based on the reduction of residual standard error and a significance level of 0.05 for variables to be included.

The prediction method corresponding to generalized-least-squares regression is called universal kriging, which is performed with the R package *spatial*. The kriging result was compared to the sum of the standard interpolation of SWE as a polynomial function of elevation, as used by the Commission for Glaciology.

A variant of universal kriging was earlier applied to spatial snowpack prediction by Erickson & Williams (2005) in the Rocky Mountains of Colorado. An alternative method, namely an additive model was used by López-Moreno (2005) in a regional-scale model for snow depth in the Spanish Pyrenees. This model class adds non-linear flexibility to regression, while running the risk of over-fitting the data (Venables & Ripley, 2002). This especially applies to rather small datasets in complex terrain as the one studied in the present work, and in the presence of spatial autocorrelation, which cannot be represented by the currently available software for additive models (Hastie & Tibshirani, 1990; Wood, 2001). Similar observations can be made for tree-based methods (Breiman, 1984; Balk & Elder, 2000; Erickson & Williams, 2005), which in addition are not continuous functions of the explanatory variables and therefore yield non-smooth prediction maps.

The spatial variability and dependence structure of SWE was analyzed using empirical correlograms of the model residuals. Correlograms represent the change (usually decrease) of correlation between pairs of measurements as the distance between the points increases

(Cressie, 1993, Goovaerts, 1997). Directional and omnidirectional correlograms were used to check for anisotropies. The correlation structure of the regression model was initially estimated from preliminary ordinary regression residuals, and later adjusted to the residuals of the selected model in order to fit a valid final model.

Statistical analyses were performed within the open-source data analysis environment R using its *spatial* and *nlme* packages (Venables & Ripley, 2002, Pinheiro et al., 2004).

4. RESULTS

4.1 Wind distribution

At the gauging station, the main wind direction during winter is from northwest to southeast, with a minor frequency in the opposite direction (figure 3). Since the station is located below the glacier, an influence of catabatic winds passing through the former glacier bed can be expected. The general atmospheric circulation coincides with the northwest direction of the winds at this station and therefore supposedly plays an additional role (figure 3). Valley wind in the opposite direction is less frequent, but reaches similar wind speeds.

Because of its high elevation and exposedness the wind system found at Schwarzkögele reflects the air flow near mountain ridges. Average and maximum wind speeds at Schwarzkögele are greatest for wind coming from the northwest sector, which contrasts with the more balanced speeds at the gauging station (figure 3).

In summary, northwesterly wind is dominant in the upper area of Vernagtferner, whereas at lower elevations catabatic and valley wind become more important. Ridges running in southwest–northeast direction may cause differences between windward and leeward sides.

4.2 Regression analysis

The exploratory analysis of the relation between SWE and elevation shows a nonlinear behavior, with increasing SWE up to ~3050 m a.s.l. and a reverse trend above this elevation, if effects of other covariables are considered (figure 4). In order to represent this relation in the regression model, elevation was centered by resting 3050 m, and an indicator variable for elevation being greater than 3050 m was introduced to model the different slopes using an interaction term.

The altitudinal trend in the three parts of Vernagtferner may be further differentiated. While there is only a weak trend in the Brochkogel area, in the opposite Schwarzwand area SWE appears to decrease above 3150 m, but these data are strongly scattered. In the central part of Vernagtferner, the Taschach area, in contrast, SWE is less scattered and strongly increases in the upper parts of the profiles. This phenomenon can best be seen and modeled in relation to the distance to the ridge that extends in windward direction above the Taschach area (figure 4).

Apart from these general trends within the study area, local-scale topographic effects in terms of curvature and wind-drift related parameters were analyzed. The curvature variable was transformed since its distribution presented large tails on both sides, and since the relation to SWE is not linear. The latter reflects the assumption that for almost straight (near-zero) curvature, small differences will have a great influence on SWE, while in strongly

convex or strongly concave areas, the same difference in curvature will have little effect on SWE. The proposed transformation first cuts down the computed curvature to the interval from -10 to +10 to eliminate artifacts, and then takes a cubic root while preserving the sign.

The residual standard errors of a regression model using the wind shelter index in combination with the other significant variables display two areas of local optimality in the index' two-dimensional parameter space (figure 5). Wind direction was taken to be northwest, and maximum distance and directional tolerance were allowed to range between 30 and 600 m and between 5° and 45°, respectively.

The global optimum is obtained for a distance parameter of 60 m and a tolerance of 15°, corresponding to rather local effects. A secondary local minimum is achieved for a distance parameter of 250 m and a tolerance of 10°, corresponding to wind transport over greater distances.

Multiple regression analysis showed furthermore that an interaction of transformed curvature with elevation is present. Specifically, the higher the elevation, the greater is the effect of curvature on SWE, while at low elevations, there is almost no effect. The combined effect of curvature and its interaction with elevation is displayed in figure 4b.

As a consequence of the overall topography, measurement distribution is unbalanced with respect to slope orientation. Exploratory analysis suggests that SWE is higher in southerly and easterly-exposed areas than in the opposite directions. A minimization of residual error with respect to cosine transformations $\cos(\text{aspect} - \text{offset})$ with varying offset directions as mentioned above showed that the best fit is reached for the measure of 'southeast-exposedness', $\cos(\text{aspect}-135^\circ)$.

4.3 Spatial variability of the snow cover

The omnidirectional residual correlogram (figure 6) shows an exponential decrease of spatial autocorrelation with distance. Autocorrelation approaches zero at a distance of ~250 m, the effective range of autocorrelation of the residual random field.

The directional empirical correlograms display a heterogeneous and irregular pattern of spatial variability. In particular, there are no clear signs of a geometric anisotropy in the main wind direction. Preference was therefore given to an isotropic correlogram.

4.4 Regression model

The regression model was selected by manually combining the mentioned transformed and untransformed variables as well as meaningful interactions between pairs of variables. The final model contains elevation, the (short-distance) wind shelter index, transformed curvature and their interaction, the interaction of elevation with the elevation threshold of 3050 m a.s.l., and a variable representing the distance to the ridge in the Taschach area. The parameter estimates of the final generalized least-squares regression are displayed in table 2. An exemplary representation of the regression surface is shown in figure 4.

While the optimal (short-distance) shelter index resulted in a significant contribution to the model fit, longer-distance versions did not add significant information in presence of the former. The 'southeast-exposedness' parameter and local slope inclination are not significant variables and were therefore dropped.

4.5 Regionalization

Universal kriging was performed based on the regression model and autocorrelation structure as fitted and described above, yielding a prediction map of SWE on Vernagtferner (figure 7). The predicted mean is 923 mm SWE and therefore 3.4% higher than the 891 mm SWE derived by the interpolation of SWE as a polynomial function of elevation. The estimated total amount of winter precipitation on Vernagtferner is $7.80 \cdot 10^9$ m³ in the case of universal kriging, and $7.54 \cdot 10^9$ m³ for the method introduced by the Commission for Glaciology. Note that for both methods the grid extend is greater than the polygon area of Vernagtferner.

5. DISCUSSION

The observed relationship between SWE and elevation, with a plateau in SWE at higher elevations, is in accordance with findings of earlier investigations on this glacier (Moser et al. 1986). This indicates a greater influence of wind redistribution at and especially deflation from these altitudes. A zone of maximum winter precipitation is not to be expected at these altitudes (Richter, 1996).

Since the effect of curvature on snow depth is essentially related to wind redistribution from convex to concave areas, the parameter estimates of curvature itself and of its interaction with elevation suggest that wind redistribution has little effect at low and great effect at high elevation. In the upper parts of Vernagtferner, the SWE at concave sites is on average ~200 mm higher than in strongly convex areas at the same altitude. This corresponds to ~50 cm of difference in snow depth.

In the Taschach area, the predominant southeastward winds transport snow from the neighbouring Gepatschferner situated northwest of the ridge to the leeward side into the upper part of this glacier. This redistribution contributes to the snow accumulation at distances of up to 600 m from the ridge. It is favoured by a rather low and open geometry of the divide, running perpendicular to the main wind direction. The mountain ridge rises about 50-100 m above the glacier, with the Sexegertenjoch and the Taschachjoch as passes in the Taschach area. Braun (1985) found highest snow accumulation on south-facing slopes leeward of mountain crests. The leeward deposited snow starts to melt at the surface and forms a crust when it freezes again. Therefore the snow is not likely to be removed by wind, even if the wind direction changes.

In the Schwarzwand and Brochkogel areas, in contrast, more complex wind flow is expected, as both the mountain ridge and the glacier slopes follow downwind directions that differ from the observed main wind direction. Thus no relation of SWE with distance to ridge in northwest-southeast direction can be found there. Regions with great snow accumulation eastwards of the mountain ridge in the Schwarzwand area at an elevation of about 3100 m suggest a greater influence of western winds there. At higher altitudes, areas with low net snow accumulation were detected. This contradicts the simplified division into leeward southeast-facing and windward northwest-facing slopes as applied in the Taschach area. Physical models of air flow may help explain the pattern of acceleration and deceleration in these areas and the corresponding deposition patterns (Bernhardt et al., 2005).

The estimated range of autocorrelation of the SWE residuals of ~250 m suggests that snow redistribution on the glacier's surface is generally restricted to this distance. The local optima of the distance parameter of the wind shelter index at 60 and 250 m, which reflect the maximum length of areas of snow deposition, are compatible with this interpretation. The

ridge distance of up to 600 m at which leeward snow accumulation takes place in the upper part of Gepatschferner, indicates that redistribution in exposed areas by strong winds may exceed the above-mentioned distances. This correlates well with results from Liston and Sturm (1998) who found that 95% of the transported snow is deposited within 500 m of distance.

Using a denser sampling design in almost glacier-free terrain, Erickson et al. (2005) found much smaller (effective) ranges of autocorrelation annually varying between ~30 and 200 m. The range parameter of the Vernagtferner at the upper end of this interval data may be due to the smoother local topography of the glacier.

A nugget effect could not be safely determined from the data due to the rather great average distances between neighbouring sampling points. Since snowfall and snow redistribution processes are continuous in space, a nugget effect should be absent if measurement error is negligible. This was assumed in the present analysis. However, due to the small range, residual variability at distances below the DEM resolution of 10 m is considerable and is an equivalent of a nugget effect at the given scale.

Regarding the overall model fit, though R^2 is not an appropriate measure of the fit in the case of correlated data, it shall be used for illustration. In an ordinary regression model with the same variables as mentioned above, an R^2 of 0.414 is achieved. This portion of explained variance reflects the great variability of snow distribution and the complex relation with environmental variables, especially the spatio-temporal wind pattern.

Slope does not play a decisive role for snow accumulation at Vernagtferner due to its small variability in the study area and in the dataset used (table 1). Slope inclination rarely

exceeds 40°. Avalanches are therefore not an important factor for snow redistribution in the study area (WITMER, 1984).

Universal kriging predicts a complex pattern of snow distribution on Vernagtferner. If only its integral, i.e. the winter mass balance, is considered, the difference to an estimate obtained using polynomial functions of elevation without process parameterization is small. The reason for this lies in the local oscillations of curvature and shelter index, which cancel out if integrated over the entire glacier, but represent important local effects in the regression model.

If the observed snow distribution pattern and model structure are representative for other years, the present analyses allow for an optimization of the sampling design for future field measurements. In order to obtain independent measurements of snow depth, a minimum distance of >250 m between sampling sites would be desirable. More detailed studies in the upper parts of the basin may furthermore be beneficial in order to better differentiate patterns of wind deposition in these areas with a strong contribution to SWE. Additional measurements of snow density will also improve the estimation of winter mass balance.

6. CONCLUSIONS

The statistical analysis of snow water equivalent revealed topographic parameters having a significant effect for snow distribution on Vernagtferner in winter 2003/2004. These parameters are related to the distribution of snowfall and its redistribution by wind. The analytical results help improve future field surveys, and provide a regionalization model that represents the present process knowledge.

For future research it is recommended that the snow accumulation data of previous years is compared with the regionalized snow accumulation pattern of 2004 in order to detect spatio-temporal variations of snow distribution. Based on these comparisons, the regionalization model may be calibrated for the estimation of winter mass balances of other years.

The estimation of the winter mass balance, however, does not yet consider the spatial variability of snow density. In order to derive a spatial distribution pattern of snow density, investigations on the spatial variability in the test site could be conducted by use of the snow micro-penetrometer (Kronholm, 2004). Thus further field research will be necessary to expand the knowledge about the distribution of both snow depth and snow density. As redistribution of snow plays a major role at Vernagtferner, further measurements of wind regime or the reconstruction of air circulation (e.g. from MM5) would be beneficial in order to model redistribution of snow in the catchment (Bernhardt et al., 2005).

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FIGURES

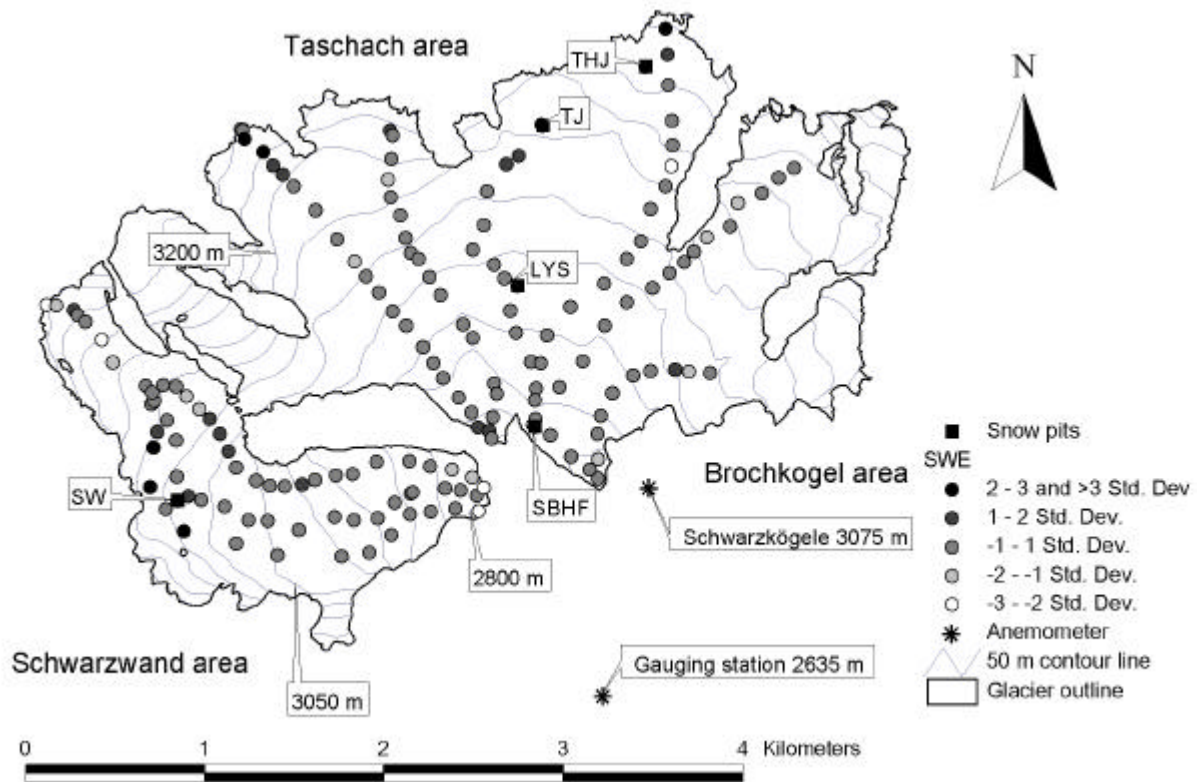


Figure 1: Vernagtferner (46°52'N, 10°49'E): Location of the 5 snow pits and 165 snow depth sample sites during field work from 29 April to 2 May 2004, and location of two anemometers in the catchment.

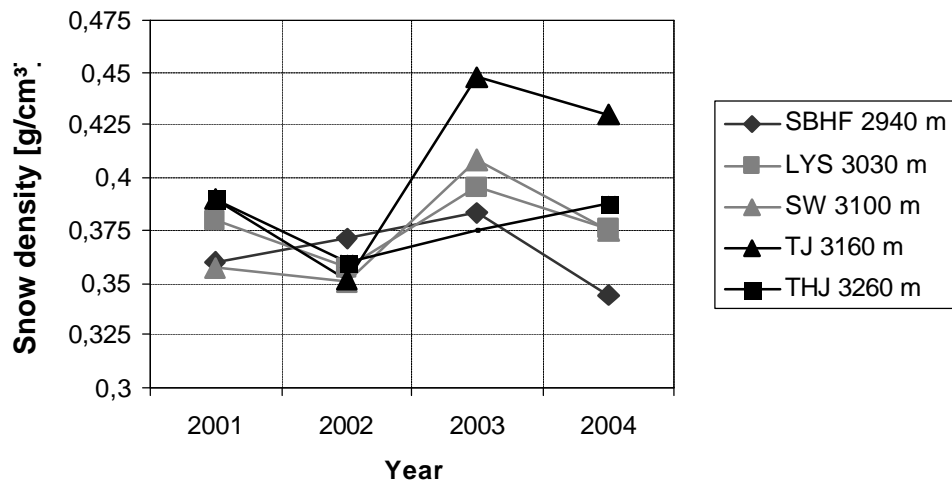


Figure 2: Snow density at the snow pits measured at the end of the accumulation period in years 2001-2004. Location of the pits can be seen in figure 1. Note: No measurement was taken at pit THJ in 2003.

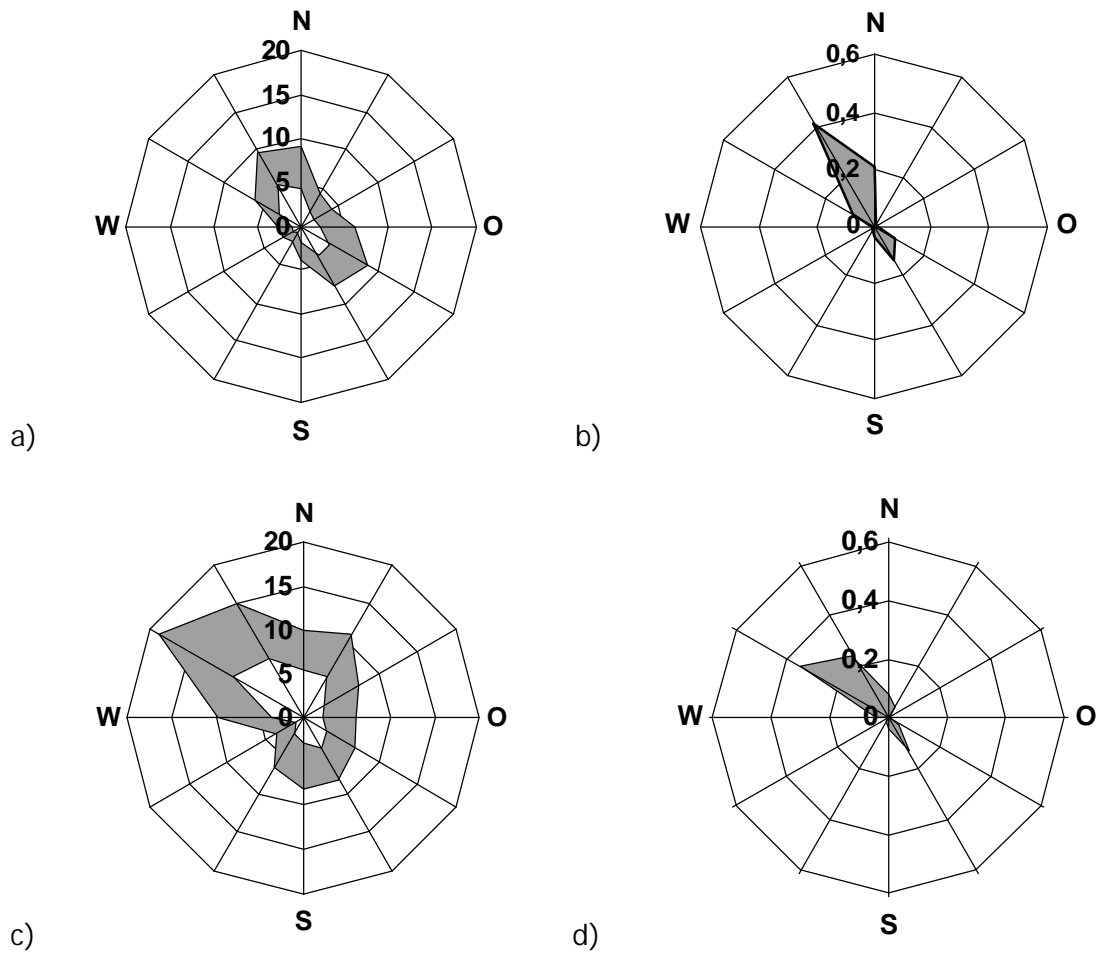


Figure 3: Wind speeds and frequencies at the gauging station (a-b) and at the Schwarzkögele peak (c-d) in winter 2003/04. Panels a and c show maximum (dark gray) and averaged (white) wind speeds [km/h] in 12 wind directions. Panels c and d display the frequency distribution of wind direction for wind speed >10 km/h. The location of the measurement sites is shown in figure 1.

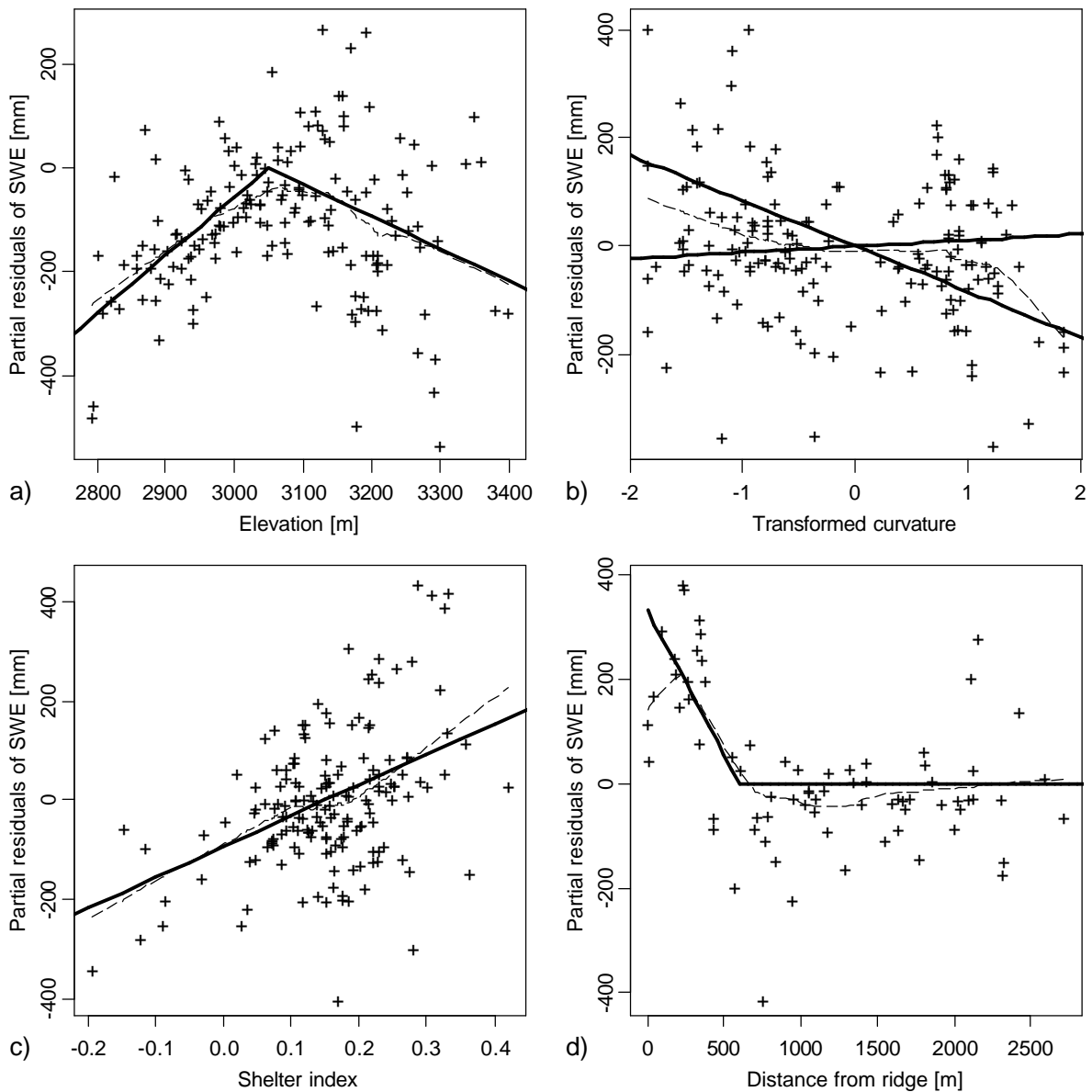


Figure 4: Scatter plots of partial SWE residuals versus explanatory model variables. The dashed lines represent univariate non-parametric smoothers, the solid lines are sections of the linear regression prediction surface. In panel b, representing curvature and its interaction with elevation, the descending line represents high-elevation areas, and the slightly ascending one low elevations. Partial residuals corresponding to selected explanatory variables refer to the part of SWE that is not explained by a model in which the corresponding coefficients are set to zero. Panel d displays only data from the Taschach area.

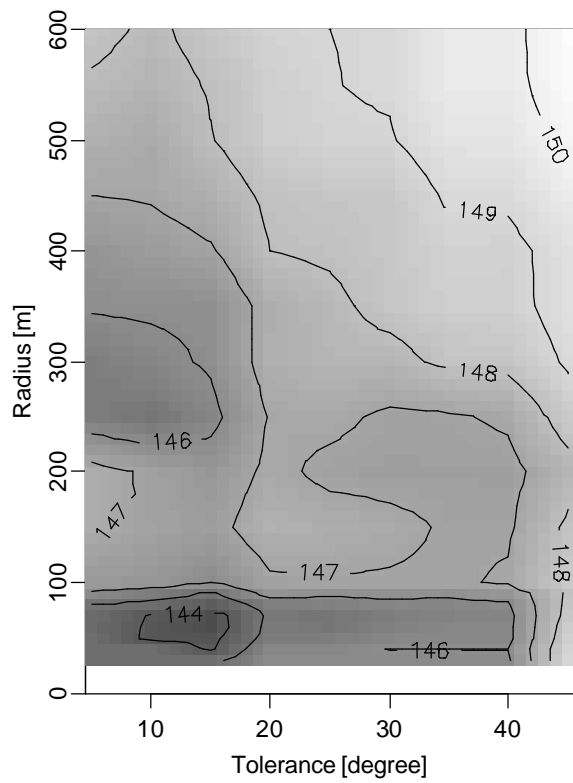


Figure 5: Residual standard errors of the model for the parameter space of the maximum distance and directional tolerance parameters of the wind shelter index. Wind direction was taken to be northwest. The parameter space is discretized in 5° steps in the tolerance dimension and in 10 m (up to 100 m distance) and 50 m steps (>100 m distance) in the case of the distance parameter.

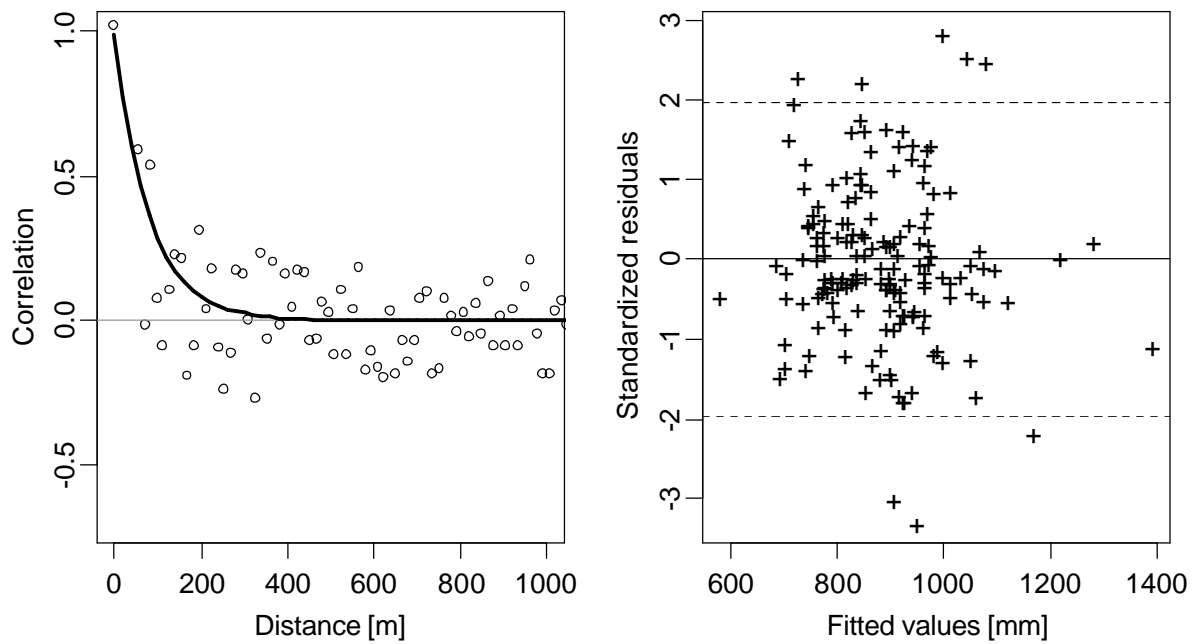


Figure 6: Left: Omnidirectional empirical correlogram of linear regression residuals (crosses), and the fitted isotropic exponential correlogram model. The effective range of autocorrelation is of ~250 m. Right: Plot of standardized model residuals.

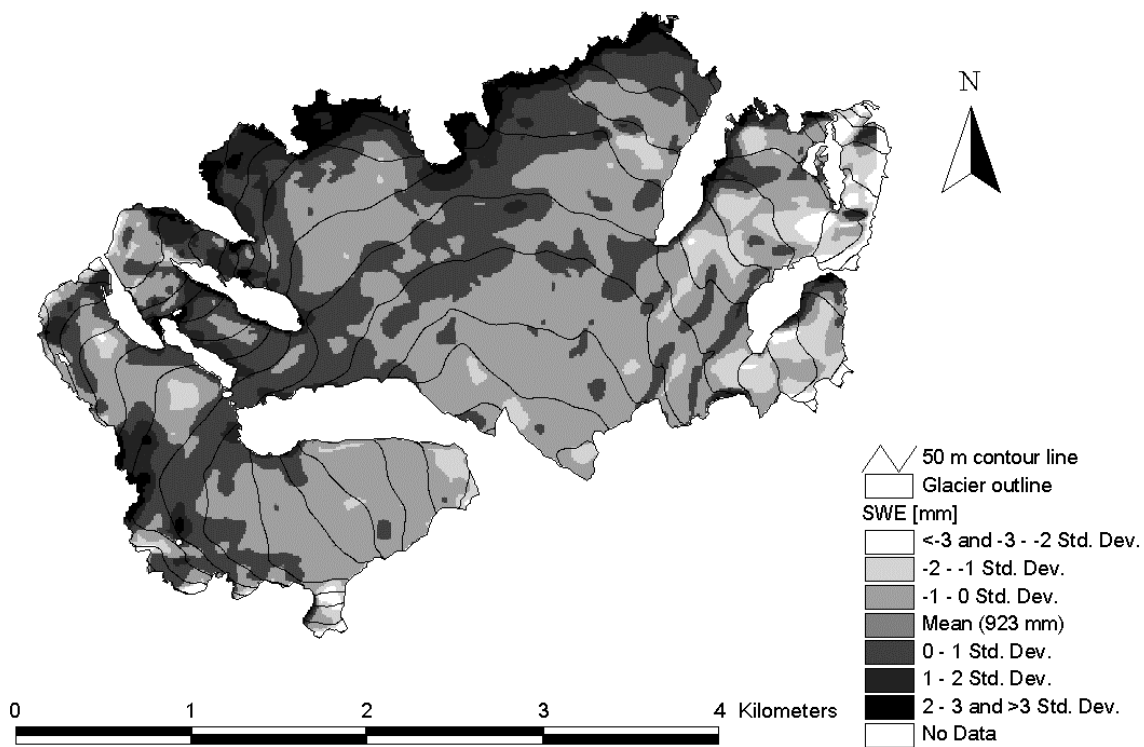


Figure 7: SWE [mm] at Vernagtferner ($46^{\circ}52'N$, $10^{\circ}49'E$) derived from universal kriging.

TABLES

<i>Variable</i>	<i>Mean \pm Std. dev.</i>	<i>Range</i>
SWE [mm]	881 \pm 164	510 – 1395
Elevation [m a.s.l.]	3068 \pm 138	2791 – 3399
Slope [°]	6.9 \pm 2.3	2.7 – 14.5
Distance from ridge in NW [m]	989 \pm 735	0 – 2787
Shelter index	0.15 \pm 0.10	-0.20 – 0.42
Curvature	-0.44 \pm 3.44	-10 – 10
Southeast-exposedness	0.45 \pm 0.41	-1.10 – 0.85

Table 1: Summary of the data used in the regression model.

<i>Variable</i>	<i>Coefficient</i>	<i>P value</i>
Intercept	858.887	0.000
Elevation	-0.627	0.008
Transformed curvature	-26.951	0.024
Transformed distance	0.555	0.000
Shelter index	621.139	0.000
Elevation * Transf. Curvature	-0.191	0.007
Elevation * (Elevation > 3050 m)	1.754	0.000
Effective range of autocorrelation [m]	250	-
Winder shelter range parameter [m]	60	-

Table 2: Estimated model parameters of the linear regression using generalized least squares and an exponential correlogram. The elevation was centered by resting 3050 m.